

**Attendance Problems.** Find the distance between each pair of points. If necessary, round your answer to the nearest hundredth.

1.  $(6, 2)$  &  $(-3, -2)$

2.  $(4, 5)$  &  $(0, 2)$

3.  $(8, 1)$  &  $(3, 6)$

4. Fill in the table of values for the equation  $y = x - 14$ .

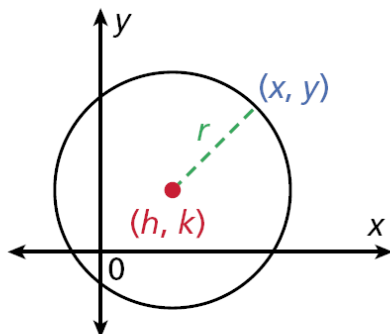
$x$	$-1$	$0$	$1$	$2$
$y$				

- I can write equations and graph circles in the coordinate plane.
- I can use the equation and graph of a circle to solve problems.

**Common Core: CC.9-12.G.GPE.1** Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.

"Worry is interest on money never borrowed."—*Unknown*

The equation of a circle is based on the Distance Formula and the fact that all points on a circle are equidistant from the center.



$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

*Distance Formula*

$$r = \sqrt{(x - h)^2 + (y - k)^2}$$

*Substitute the given values.*

$$r^2 = (x - h)^2 + (y - k)^2$$

*Square both sides.*

### **Theorem 11-7-1** Equation of a Circle

The equation of a circle with center  $(h, k)$  and radius  $r$  is  $(x - h)^2 + (y - k)^2 = r^2$ .



**1 Writing the Equation of a Circle**

Write the equation of each circle.

**A**  $\odot A$  with center  $A(4, -2)$  and radius 3

$$(x - h)^2 + (y - k)^2 = r^2 \quad \text{Equation of a circle}$$

$$(x - 4)^2 + (y - (-2))^2 = 3^2 \quad \text{Substitute 4 for } h, -2 \text{ for } k, \text{ and 3 for } r.$$

$$(x - 4)^2 + (y + 2)^2 = 9 \quad \text{Simplify.}$$

**B**  $\odot B$  that passes through  $(-2, 6)$  and has center  $B(-6, 3)$

$$r = \sqrt{(-2 - (-6))^2 + (6 - 3)^2} \quad \text{Distance Formula}$$

$$= \sqrt{25} = 5 \quad \text{Simplify.}$$

$$(x - (-6))^2 + (y - 3)^2 = 5^2 \quad \text{Substitute } -6 \text{ for } h, 3 \text{ for } k, \text{ and 5 for } r.$$

$$(x + 6)^2 + (y - 3)^2 = 25 \quad \text{Simplify.}$$

**Example 1.** Write the equation of each circle.

A.  $\odot J$  with center  $J(2, 2)$  and radius 4.

**B.**  $\odot K$  that passes through  $J(6, 4)$  & has center  $K(1, -8)$

**Guided Practice. Write the equation of each circle.**

- 4.**  $\odot P$  with center  $P(0, -3)$  and radius 8.

5.  $\odot Q$  that passes through  $(2, 3)$  and has center  $Q(2, -1)$ .

If you are given the equation of a circle, you can graph the circle by making a table or by identifying its center and radius.

## 2 Graphing a Circle

Graph each equation.

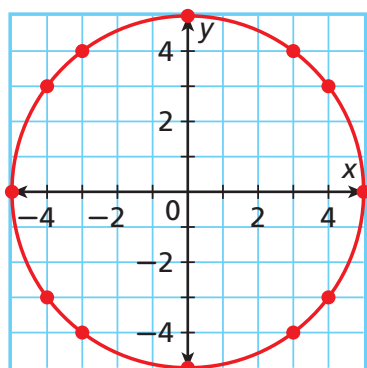
**A**  $x^2 + y^2 = 25$

**Step 1** Make a table of values.

Since the radius is  $\sqrt{25}$ , or 5, use  $\pm 5$  and the values between for  $x$ -values.

$x$	-5	-4	-3	0	3	4	5
$y$	0	$\pm 3$	$\pm 4$	$\pm 5$	$\pm 4$	$\pm 3$	0

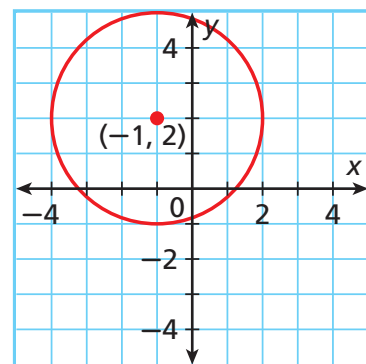
**Step 2** Plot the points and connect them to form a circle.



**B**  $(x + 1)^2 + (y - 2)^2 = 9$

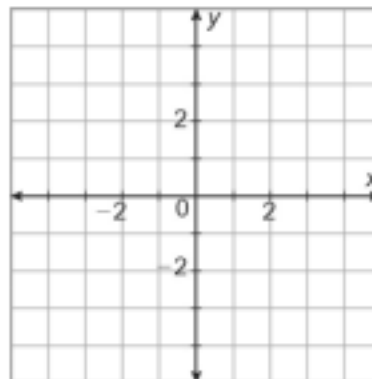
The equation of the given circle can be written as  $(x - (-1))^2 + (y - 2)^2 = 3^2$ . So  $h = -1$ ,  $k = 2$ , and  $r = 3$ .

The center is  $(-1, 2)$ , and the radius is 3. Plot the point  $(-1, 2)$ . Then graph a circle having this center and radius 3.

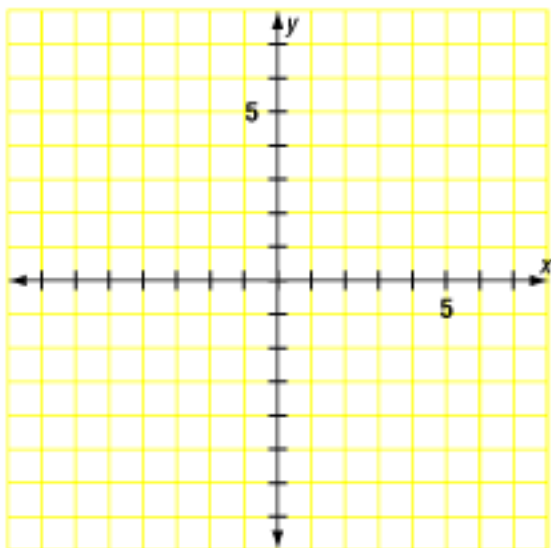


**Example 2. Graph the following**

A.  $x^2 + y^2 = 16$

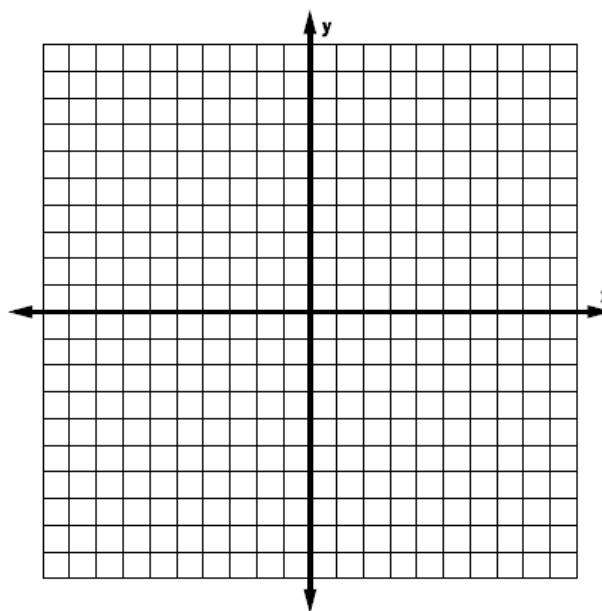


B.  $(x - 3)^2 + (y + 4)^2 = 9$



**6. Guided Practice.** Graph

$(x - 3)^2 + (y + 2)^2 = 4$



### 3 Meteorology Application

Meteorologists are planning the location of a new weather station to cover Osceola, Waco, and Ireland, Texas. To optimize radar coverage, the station must be equidistant from the three cities which are located on a coordinate plane at  $A(2, 5)$ ,  $B(3, -2)$ , and  $C(-5, -2)$ .

- What are the coordinates where the station should be built?
- If each unit of the coordinate plane represents 8.5 miles, what is the diameter of the region covered by the radar?

**Step 1** Plot the three given points.

**Step 2** Connect  $A$ ,  $B$ , and  $C$  to form a triangle.

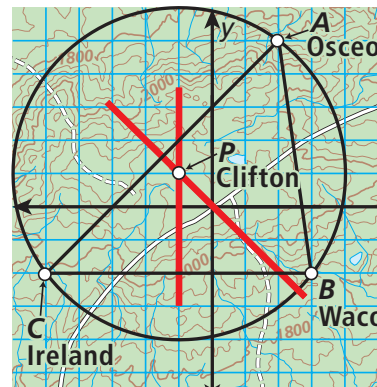
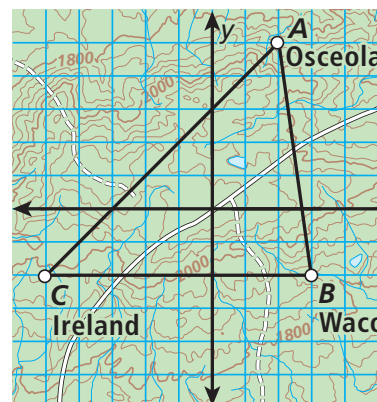
**Step 3** Find a point that is equidistant from the three points by constructing the perpendicular bisectors of two of the sides of  $\triangle ABC$ .

The perpendicular bisectors of the sides of  $\triangle ABC$  intersect at a point that is equidistant from  $A$ ,  $B$ , and  $C$ .

The intersection of the perpendicular bisectors is  $P(-1, 1)$ .  $P$  is the center of the circle that passes through  $A$ ,  $B$ , and  $C$ .

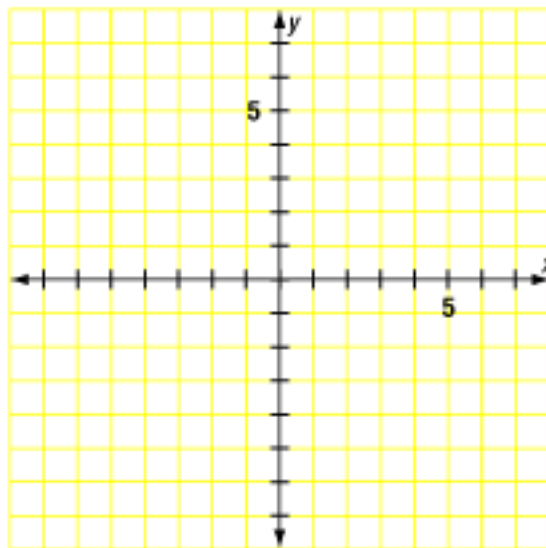
The weather station should be built at  $P(-1, 1)$ , Clifton, Texas.

There are approximately 10 units across the circle. So the diameter of the region covered by the radar is approximately 85 miles.

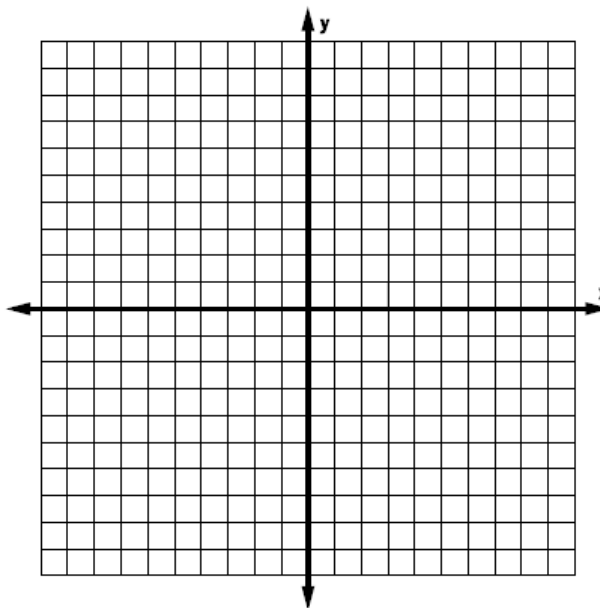




**Example 3:** An amateur radio operator wants to build a radio antenna near his home without using his house as a bracing point. He uses three poles to brace the antenna. The poles are to be inserted in the ground at three points equidistant from the antenna located at  $J(4, 4)$ ,  $K(-3, -1)$ , and  $L(2, -8)$ . What are the coordinates of the base of the antenna?



**7. Guided Practice.** Suppose the coordinates of the three cities in Example 3 (p. 801) are  $D(6, 2)$ ,  $E(5, -5)$ , and  $F(-2, -4)$ . What would be the location of the weather station?



### **12-7 Circles in the Coordinate Plane**

- Mickey Mouse Graph in Desmos
- (p 850) 18, 24, 28, 29, 34, 36, 38, 41.
- 12B Ready to Go On pretest & posttests.